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# Hydrodynamic dimensions of heteroarm star copolymers by size exclusion chromatography

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## Abstract

Heteroarm star copolymers, i.e. star-shaped polymers bearing A and B pure arms (type  $A_nB_n$ ) were synthesized by anionic polymerization and their hydrodynamic properties in a common good solvent were investigated by means of size exclusion chromatography. The proposed method allows the study of the evolution of the hydrodynamic dimensions of the heteroarm star copolymers as the second generation of the arms is growing from the cores. Different growth rates of the  $A_nB_n$  star size were observed which are influenced by three factors: the number of arms, the ratio of the size of the chemically different arms and the interactions between the unlike segments. The last factor is affected significantly by the selectivity of the solvent. © 1999 Elsevier Science Ltd. All rights reserved.

Keywords: Heteroarm star copolymers; Size exclusion chromatography; Hydronamic dimensions

## 1. Introduction

Star-shaped block copolymers exhibiting novel architectures have been synthesized by "living" polymerization techniques and the study of their properties in solution as well as in the bulk, has received much attention in the recent years [1-5].

Our efforts have been focused on the heteroarm star copolymers which are star-shaped macromolecules constituted from a central poly(DVB) core bearing equal number of A and B arms (type  $A_nB_n$ ) [1,6–8].

Their synthesis is performed via an anionic copolymerization method comprising three sequential steps [1]. In the first two steps a star-shaped polymer ( $A_n$ ) is formed by reacting a living linear precursor (arms A) with a bisunsaturated monomer (e.g. divinylbenzene). The resulting star polymer is still "living", bearing within its core a number of "living' sites equal to the number of the arms incorporated in the star molecule. These sites are able to initiate the polymerization of another suitable monomer. In the third step a new set of arms is growing from the core yielding the heteroarm star copolymer ( $A_nB_n$ ).

Recently the solution properties of the heteroarm star copolymers, in common good solvents as well as in selective solvents have been reported [7,9-15]. As have been

shown, the architecture of the macromolecule plays an important role on the micellar properties of block copolymers. Critical micelle concentrations, aggregation numbers, hydrodynamic dimensions and microdomain sizes of micelles afforded by star-shaped  $A_nB_n$  copolymers differ remarkably from those afforded by the linear AB diblock copolymers.

The aim of the present article is firstly to report on the solution properties of the  $A_nB_n$  heteroarm star copolymers in a common good solvent for the different arms and secondly to show how one can use the size exclusion chromatography to obtain information concerning the hydrodynamic dimensions of these macromolecules with the specific topology. Especially we look how the molecular characteristics of the star copolymers such as the different arms length ratio, the number of arms and the interactions between the unlike segments influence the hydrodynamic size of the  $A_nB_n$  star copolymer.

## 2. Experimental part

## 2.1. Synthetic procedure

All the heteroarm star copolymers were synthesized by anionic polymerization under argon atmosphere using THF as solvent. The procedure used is a three step sequential "living" copolymerization method which allows the

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Fig. 1. Absorbance at  $1730 \text{ cm}^{-1}$  as a function of the concentration of poly(ethyl methacrylate).

preparation, from the same reaction, of a series of star copolymers differing only in the length of the second generation of arms (PEMA, PtBA and P2VP).

In the first step the PS arms were synthesized, using secbutyl lithium as initiator, at  $-40^{\circ}$ C in the presence of LiCl. In the second step a small amount of DVB was polymerized by the living polystyril lithium chains, yielding star-shaped polystyrene (PS<sub>n</sub>). These star polymers are still "living", bearing a number of active sites equal to the number of their arms. In the third step these active sites are used to polymerize another monomer such as ethylmethacrylate (EMA), tert-butyl acrylate (tBA) and 2-vinylpyridine (2VP). The polymerization of EMA and tBA was carried out at  $-60^{\circ}$ C and for 2VP at  $-78^{\circ}$ C. In this step parts of the

Table 1 Characterization data of PS<sub>n</sub>PEMA<sub>n</sub> copolymers

reaction mixture were withdrawn following every time the addition of another amount of monomer. The active sites were deactivated by the addition of degassed methanol. Moreover, in every synthesis an appropriate amount of solution was sampled out after the completion of styrene and DVB polymerization, for the purpose of characterization. The PS<sub>n</sub>PEMA<sub>n</sub> and PS<sub>n</sub>PtBA<sub>n</sub> copolymers were precipitated in a methanol/water mixture (80/20, v/v) and the PS<sub>n</sub>P2VP<sub>n</sub> copolymers in cold heptane.

#### 2.2. Characterization

The  $M_w$  of the PS arms was obtained by SEC using PS standards. The  $M_w$  of the PS<sub>n</sub> was determined by multiangle laser light scattering in THF at 25°C using the model SEM RD spectrogoniometer (Sematech, France) equipped with a He–Ne laser (633 nm). The weight average functionality *n* of the PS<sub>n</sub> was calculated by the equation

$$n = \frac{M_{\rm w}({\rm PS}_n)}{M_{\rm w}({\rm PS}_{\rm arm}) + m_{\rm o}[{\rm DVB}]/[{\rm LE}]}$$
(1)

where  $m_0$  is the molecular weight of divinyl benzene and [DVB]/[LE] is the divinylbenzene per living ends mole ratio.

The weight content, *W*, of PEMA and PtBA in  $PS_nPEMA_n$ and  $PS_nPtBA_n$  copolymers respectively was determined by IR spectroscopy which was carried out on a Perkin–Elmer 16PC apparatus. The polymer solutions in CCl<sub>4</sub> were recorded with a NaCl cell. The carbonyl group of PEMA and PtBA gives a very strong and narrow absorption in the infrared region at 1730 cm<sup>-1</sup>. Subsequently FTIR spectroscopy can be used to determine the PEMA and PtBA content of the copolymers. The procedure consisted in calibrating a NaCl cell with PEMA and PtBA homopolymer solutions in CCl<sub>4</sub> and determining the absorbance  $A_{1730}$  of a solution of the copolymer of known concentration in the same cell. The plot of absorbance at 1730 cm<sup>-1</sup> as a function of the

Sample <sup>a</sup>	$M_{\rm w}$ (PS <sub>arm</sub> ) (×10 <sup>-4</sup> g/mol)	$M_{\rm w}$ (PS <sub>n</sub> ) (×10 <sup>-4</sup> g/mol)	п	$W_{\text{PEMA}}$ (%)	$M_{\rm w}$ (PEMA <sub>arm</sub> ) (× 10 <sup>-4</sup> g/mol)
PS <sub>4</sub> PEMA <sub>4</sub> 26	2.6	11.7	4.4	26.0	0.93
PS <sub>4</sub> PEMA <sub>4</sub> 50	2.6	11.7	4.4	50.45	2.70
PS <sub>4</sub> PEMA <sub>4</sub> 58	2.6	11.7	4.4	57.9	3.66
PS <sub>4</sub> PEMA <sub>4</sub> 62	2.6	11.7	4.4	62.3	4.39
PS <sub>4</sub> PEMA <sub>4</sub> 67	2.6	11.7	4.4	67.3	5.46
PS <sub>6</sub> PEMA <sub>6</sub> 19	3.4	24.1	6.3	18.95	0.89
PS <sub>6</sub> PEMA <sub>6</sub> 37	3.4	24.1	6.3	36.5	2.20
PS <sub>6</sub> PEMA <sub>6</sub> 52	3.4	24.1	6.3	52.3	4.19
PS <sub>6</sub> PEMA <sub>6</sub> 57	3.4	24.1	6.3	56.7	5.02
PS <sub>6</sub> PEMA <sub>6</sub> 61	3.4	24.1	6.3	60.9	5.95
PS <sub>0</sub> PEMA <sub>0</sub> 19	2.0	20.0	9.0	18.5	0.50
PS <sub>0</sub> PEMA <sub>0</sub> 36	2.0	20.0	9.0	36.4	1.27
PS <sub>0</sub> PEMA <sub>0</sub> 51	2.0	20.0	9.0	50.9	2.30
PS <sub>0</sub> PEMA <sub>0</sub> 59	2.0	20.0	9.0	58.9	3.19
PSoPEMA63	2.0	20.0	9.0	62.5	3 70

<sup>a</sup>  $A_n B_n W$ : A and B are the kind of arms, n stands for the weight average functionality and W the weight content of PEMA in the copolymers.

Table 2			
Characterization d	lata of	PS.,PtBA.,	copolymers

Sample <sup>a</sup>	$M_{\rm w}$ (PS <sub>arm</sub> ) (×10 <sup>-4</sup> g/mol)	$M_{\rm w}$ (PS <sub>n</sub> ) (× 10 <sup>-4</sup> g/mol)	п	$W_{\text{PtBA}}$ (%)	$M_{\rm w}$ (PtBA <sub>arm</sub> ) (×10 <sup>-4</sup> g/mol)
PS <sub>4</sub> PtBA <sub>4</sub> 26	2.8	13.8	4.7	26.0	1.03
PS <sub>4</sub> PtBA <sub>4</sub> 40	2.8	13.8	4.7	39.9	1.95
PS <sub>4</sub> PtBA <sub>4</sub> 48	2.8	13.8	4.7	47.7	2.68
PS <sub>4</sub> PtBA <sub>4</sub> 53	2.8	13.8	4.7	53.3	3.35
PS <sub>4</sub> PtBA <sub>4</sub> 56	2.8	13.8	4.7	56.4	3.82

<sup>a</sup>  $A_n B_n W$ : the same as in Table 1, where W stands for the weight content of PtBA in the copolymers.

concentration of PEMA or PtBA is a straight line (r = 0.999) (Fig. 1), as expected from the Beer–Lambert law. Thus *W* was calculated from the equation

$$W = \frac{A_{1730}}{bc} \tag{2}$$

where *b* is the slope of calibration curve and *c* the concentration in  $g/100 \text{ cm}^3$ .

The weight content of P2VP in  $PS_nP2VP_n$  copolymers was determined by <sup>1</sup>H NMR from the integrated peak intensities corresponding to the *a* proton in the aromatic pyridine group (8.0–8.3 ppm) compared to the rest of the aromatic protons (6.3–7.4 ppm). The <sup>1</sup>H NMR spectra of  $PS_nP2VP_n$ diluted in CDCl<sub>3</sub> were recorded on a Bruker AMX-400 (400 MHz) spectrometer.

Provided that the PS and PEMA arms are equal, the molecular weight of the PEMA arms can be calculated by the formula

$$M_{\rm w}({\rm PEMA}_{\rm arm}) = \frac{M_{\rm w}({\rm PS}_n)W_{\rm PEMA}}{n(1 - W_{\rm PEMA})}.$$
(3)

In the case of  $PS_nPtBA_n$  and  $PS_nP2VP_n$  copolymers PEMA in Eq. (3) is replaced by PtBA and P2VP respectively. The molecular characteristics of heteroarm star copolymers are given in Tables 1–3.

#### 2.3. Size exclusion chromatography (SEC)

SEC was carried out using a model 201 apparatus equipped with a model 401 differential refractometer as detector (Water Associates). A set of three  $\mu$ -Styragel columns (10<sup>3</sup>, 10<sup>4</sup> and 10<sup>5</sup> Å) was used and the calibration curve was obtained by PS standards. The mobile phase was tetrahydrofuran (analytical grade) and the flow rate was 1 cm<sup>3</sup> min<sup>-1</sup>. In the case of PS<sub>n</sub>P2VP<sub>n</sub> copolymers SEC

Table 3			
Characterization	data	of $PS_nP2VP_n$	copolymers

Sample <sup>a</sup>	$M_{\rm w}$ (PS <sub>arm</sub> ) (× 10 <sup>-4</sup> g/mol)	$M_{\rm w}$ (PS <sub>n</sub> ) (× 10 <sup>-4</sup> g/mol)	п	$W_{\mathrm{P2VP}}$ (%)	$M_{\rm w} \ ({\rm P2VP_{arm}}) \ (\times 10^{-4} \ {\rm g/mol})$
PS <sub>6</sub> P2VP <sub>6</sub> 24	2.3	15.6	6.1	24	0.81
PS <sub>6</sub> P2VP <sub>6</sub> 44	2.0	15.4	6.9	44	1.75
$PS_6P2VP_660$	2.0	15.4	6.9	60	4.33
PS <sub>6</sub> P2VP <sub>6</sub> 66	2.0	15.4	6.9	66	4.33

<sup>a</sup>  $A_n B_n W$ : the same as in Table 1, where W stands for the weight content of P2VP in the copolymers.

was performed with a mixture of tetrahydrofuran and triethylamine (THF/Et<sub>3</sub>N, 99/1, v/v) to prevent adsorption of P2VP in the columns.

### 3. Results and discussion

SEC is a chromatographic technique for which the separation mechanism relies on the size of the macromolecules under analysis. In the case where interactions between the macromolecule and the sorbent are negligible the retention volume  $V_{\rm R}$  of a macromolecule is related to its hydrodynamic dimensions.

According to the universal calibration concept the chromatographic data can be evaluated through the relationship

$$\log V_{\rm h} = A' - B' V_{\rm R} \tag{4}$$

where  $V_{\rm h}$  is the hydrodynamic volume of the macromolecules and A', B' are constants related every time to the chromatographic system. For the heteroarm star copolymer,  $A_nB_n$ , and the star precursor it originated from,  $A_n$ , Eq. (4) can be written as

$$\log V_{\rm h}^{**} = A' - B' V_{\rm R}^{**} \tag{5}$$

and

$$\log V_{\rm h}^* = A' - B' V_{\rm R}^* \tag{6}$$

where superscripts \* and \*\* denote  $A_n$  and  $A_nB_n$  star respectively. Subtracting Eqs. (5) and (6) we obtain

$$\log \frac{V_{\rm h}^{**}}{V_{\rm h}^*} = B' \Delta V_{\rm R} \tag{7}$$

where  $\Delta V_{\rm R} = V_{\rm R}^* - V_{\rm R}^{**}$ . Therefore the difference between the retention volumes of the  $A_n B_n$  star and its  $A_n$  star precursor, reflects their hydrodynamic volume ratio (i.e.



Fig. 2. GPC chromatograms of (a) IPS, (b)  $PS_n$  and (c)–(g)  $PS_9PEMA_9$  copolymers with increasing  $W_{PEMA}$ .

normalized hydrodynamic volume of the heteroarm star) and is used to monitor the evolution of the hydrodynamic dimensions of the heteroarm star copolymers with respect to the growing second generation of arms (B). Previous results have shown that in some cases the hydrodynamic dimensions of  $A_nB_n$  remain the same with those of  $A_n$ , although a new set of arms have been growing from the core [7]. On the other hand, in other systems  $A_nB_n$  shows significant augmentation of its hydrodynamic dimensions upon the addition of the B arms [6].

In order to elucidate the factors which affect the overall dimensions of the heteroarm star copolymer in solution, a

number of series of  $A_nB_n$  star copolymer were synthesized. In each series, the number, the length and the nature of the A arms were kept constant while the length and/or the nature of the B arms is varied. In Fig. 2 a number of chromatograms corresponding to a series of PS<sub>n</sub>PEMA<sub>n</sub> star copolymers together with the PS<sub>n</sub> star precursor and the PS (linear) arms are presented.

As it is seen together with the main peak of the  $A_nB_n$  star copolymer a small peak exists which coincides with the peak corresponding to the PS linear precursor (arms). This linear residual arises from accidental deactivation during the formation of the PS<sub>n</sub> star at the second step of the synthetic procedure. The presence of these residues can be ignored in our analysis and this is one of the benefits of the present method. Our attention focuses on the behavior of the  $V_R$  (on peak) of the  $A_nB_n$  stars.

Two ways could be applied to evaluate the chromatographic data of Fig. 2. Firstly, we use the difference  $\Delta V_R$ which according to Eq. (7) expresses the normalized hydrodynamic volume of the  $A_nB_n$  star with respect to that of the  $A_n$  precursor. In Fig. 3(a)  $\Delta V_R$  is plotted as a function of the PEMA weight percentage for three the series of PS<sub>n</sub>PEMA<sub>n</sub> differing on the number of arms.

Secondly the overall dimensions of the star copolymers can be evaluated by converting the primary calibration curve obtained with the PS linear standards

$$\log M = 11, 12 - 0,284V_{\rm R} \tag{8}$$

to a universal type calibration curve in terms of the hydrodynamic radius  $R_{\rm H}$  (nm) by using the scaling relationship valid for the PS/THF system [16]



Fig. 3. (a) Variation of  $\Delta V_R$  versus  $W_{\text{PEMA}}$  and (b)  $R_H$  versus  $W_{\text{PEMA}}$ , for the three  $\text{PS}_n\text{PEMA}_n$  copolymers series. The inset shows the percentage increase of  $R_H$  as a function of the star functionality n, when the molecular weight of the  $\text{PS}_n\text{PEMA}_n$  copolymers is double with respect to  $\text{PS}_n$  ( $W_{\text{PEMA}} = 50\%$ ).



Fig. 4. Schematic representation of the size increase of  $A_n B_n$  copolymers as the second set of arms are growing from the core.

(9)

 $R_{\rm H} = (1.37 \times 10^{-2}) M^{0.564}$ 

therefore Eq. (8) becomes

$$\log R_{\rm H} = 4.408 - 0.16 V_{\rm R}.$$
 (10)

In Fig. 3(b) the overall dimensions in terms of hydrodynamic radius, obtained by using Eq. (10) for the three series of PS<sub>n</sub>PEMA<sub>n</sub> star copolymers differing on the number of arms, have been plotted as a function of the PEMA weight percentage. In fact, Fig. 3(a) and (b) demonstrates the evolution of the hydrodynamic dimensions of a  $PS_n$  star macromolecule as a new set of PEMA branches are growing from its core leading to  $PS_nPEMA_n$ . As it can be observed different  $V_{\rm h}$  growth rates occur depending on the star functionality n. Several different stages can be distinguished which are presented schematically in Fig. 4. In stage 0 the hydrodynamic size of the star polymer is determined from the number of the PS arms and the length of each arm. In stage 1, where the length of the PEMA arms are still short the overall dimensions remain unaltered. For the  $PS_n$  with n = 4.4 stage 1 is extended up to 25%  $W_{\text{PEMA}}$  while for the other samples with higher functionality this stage is shifted to lower  $W_{\text{PEMA}}$ . At stage 2, where the lengths of the different arms become comparable, there is a smooth increase of the hydrodynamic dimensions depending on the arms

Table 4 Mark-Houwink-Sakurada (MHS) equation's constants

<b>a</b>	W (1, 10 <sup>3</sup> )		• 8
System	$K (\times 10^{\circ})$	a	$\Delta \alpha^{-}$
PS/THF	16 <sup>b</sup>	0.706 <sup>b</sup>	
PEMA/THF	6.04 <sup>c</sup>	0.750 <sup>c</sup>	0.044
PtBA/THF	3.3 <sup>d</sup>	$0.800^{d}$	0.094
P2VP/THF	14.9 <sup>e</sup>	0.660 <sup>e</sup>	0.046

<sup>a</sup>  $\Delta \alpha = |\alpha_{\rm PS} - \alpha_{\rm B}|.$ 

<sup>b</sup> From Ref. [22].

<sup>c</sup> From viscosity measurements, this work.

<sup>d</sup> From Ref. [23].

<sup>e</sup> From Ref. [24].

number. In the inset of Fig. 3(b) the percentage increase of  $R_{\rm H}$ , where the molecular weight of the heteroarm star copolymer  $A_nB_n$  is double with respect to  $A_n$  it originates from ( $W_{\rm PEMA} = 50\%$ ), is plotted as a function of the star functionality *n*. As shown for n = 4.4 the  $R_{\rm H}$  value increases by only 8% while for n = 9 the increase is 33%. Obviously the dimensions of the heteroarm star copolymer are affected significantly by the number of arms.

Finally in stage 3 the length of the second generation of arms (PEMA) has exceeded that of the first generation of arms (PS) and the dimensions of  $A_nB_n$  increase now more sharply. In this case the size of the star-shaped macromolecule is determined mainly by the length of the second set of arms.

In an attempt to understand better how the hydrodynamic volume of the heteroarm star  $A_nB_n$  is influenced by the presence of the different arms, we have plotted  $\Delta V_R$  against the dimensionless ratio *L* defined as follows:

$$L = \frac{(r^2)_{\rm B}^{1/2}}{(r^2)_{\rm A}^{1/2}} \tag{11}$$

where  $(r^2)^{1/2}$  is the end-to-end distance expressing the effective size of the arms in the solution [17]

$$(r^2)^{1/2} = \Phi^{-1/3} \{ [\eta] M \}^{1/3}$$
(12)

where  $\Phi$  is a constant,  $[\eta]$  is the intrinsic viscosity and M the molar mass.

Rearranging  $[\eta]$  from the Mark–Houwink–Sakurada equation,  $[\eta] = KM^a$ , *L* can be rewritten as

$$L = \left(\frac{K_{\rm B}M_{\rm B}^{a_{\rm B}+1}}{K_{\rm A}M_{\rm A}^{a_{\rm A}+1}}\right)^{1/3}.$$
(13)

The constant  $\Phi$  of Eq. (12) is affected from the number of arms and the solvent quality. Since we use a common good solvent and the number of the different arms are equal the ratio  $\Phi_A/\Phi_B$  is close to unity and has been removed from Eq.



Fig. 5. Plot of  $\Delta V_R$  as a function of ratio *L* for the three PS<sub>n</sub>PEMA<sub>n</sub> copolymers series.

(13). L values were calculated using arm molecular weights from Tables 1–3 and MHS constants from Table 4.

Fig. 5 demonstrates the variation of  $\Delta V_R$  versus *L* for the three PS<sub>n</sub>PEMA<sub>n</sub> star copolymers series. For the sample with the lowest *n* the hydrodynamic volume of PS<sub>n</sub>PEMA<sub>n</sub> remains the same with respect to that of PS<sub>n</sub> it originates



Fig. 6. Star functionality *n* dependence of  $\Delta V_R$  passing from PS<sub>n</sub> to PS<sub>2n</sub> ( $\bullet$ ) and from PS<sub>n</sub> to PS<sub>n</sub>PEMA<sub>n</sub> ( $\blacksquare$ ). The inset shows the star functionality *n* dependence of  $V_R$  for PS<sub>n</sub> with  $M_{br} = 20\ 000$ , calculated by the Eqs. (8) and (14). The solid lines, in the inset, express the  $\Delta V_R$  passing from PS<sub>4</sub> to PS<sub>8</sub> and from PS<sub>9</sub> to PS<sub>18</sub>.

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Calculated and experimental values of  $V_R$  and  $\Delta V_R$  for PS<sub>n</sub>, PS<sub>2n</sub> and PS<sub>n</sub>PEMA<sub>n</sub> (W<sub>PEMA</sub> = 50%) samples

Sample	$V_{\rm R}$ (ml)		$\Delta V_{\rm R}$ (ml)		
	Calculated <sup>a</sup>	Experimental <sup>b</sup>	Calculated <sup>a</sup>	Experimental <sup>c</sup>	
PS <sub>4</sub>	21.69	21.85			
$PS_8$	21.05		0.64		
PS <sub>4</sub> PEMA <sub>4</sub>				0.4	
PS <sub>6</sub>	20.93	20.91			
$PS_{12}$	20.36		0.57		
PS <sub>6</sub> PEMA <sub>6</sub>				0.56	
PS <sub>9</sub>	21.43	21.36			
PS <sub>18</sub>	20.95		0.48		
PS <sub>9</sub> PEMA <sub>9</sub>				0.95	

<sup>a</sup> From Eqs. (8) and (14).

<sup>b</sup> From SEC.

<sup>c</sup> From interpolation to Fig. 5.

from until the effective length of the PEMA arms reaches about 45% of that of the PS arm (stage 1, Fig. 4). Accordingly the hydrodynamic volume increases smoothly until the PEMA arms reach 85% of the PS arm length (stage 2) and finally the  $V_h$  of  $A_n B_n$  increases further with a higher rate (stage 3).

The hydrodynamic volume for the star polymers with higher number of arms increases more rapidly due to the fact that the segment density increases making the repulsive interactions between the unlike segments of the different arms more effective. This can be demonstrated by plotting  $\Delta V_{\rm R}$  at L = 1 (where the effective length of the different arms becomes equal) as a function of the star functionality n (Fig. 6).

In the same plot the  $V_R$  difference between the  $PS_n$  and another star polymer having double number of arms  $(PS_{2n})$ of the same arm length is also shown. The  $V_R$  of the  $PS_{2n}$  has been calculated by using the equation

$$M_{\rm s} = M_{\rm br} \cdot n \left[ \frac{3n-2}{n^2} \right]^{\varepsilon/\alpha+1} \left[ \frac{1-0.276-0.015(n-1)}{1-0.276} \right]^{1/\alpha+1}$$
(14)

where  $M_s$  is the molecular weight of a linear polymer standard which is eluted at the same retention volume with a star-shaped polymer homolog, having *n* number of arms of  $M_{br}$  molecular weight, *a* is the MHS exponent of the polymer (standard) solvent system under analysis and  $\varepsilon$  the exponent of the equation  $g = g^{\varepsilon}$  (where g', g are the branching factors) [18]. Therefore  $V_R$  can be calculated by using the conventional calibration curve established by linear PS standards (Eq. (8)). The  $V_R$  data are collected in Table 5. We see that the calculated values are in excellent agreement with the experimental ones, confirming the validity of Eq. (14).

As shown in Fig. 6 the variation of the dimensions of a homoarm star from  $PS_n$  to  $PS_{2n}$  decreases with the star functionality. This is expected since  $V_R$  of a star-shaped polymer



Fig. 7. Plot of  $\Delta V_R$  as a function of ratio L for (a) PS<sub>n</sub>PEMA<sub>n</sub>, PS<sub>n</sub>PtBA<sub>n</sub> and (b) PS<sub>n</sub>PEMA<sub>n</sub>, PS<sub>n</sub>P2VP<sub>n</sub>.

decreases exponentially with the star functionality as shown in the inset of Fig. 6. On the contrary,  $\Delta V_{\rm R}$  increases in the case of the heteroarm stars passing from  $PS_n$  to  $PS_nPEMA_n$ due to an increase of the heterocontacts between the different arms and therefore provoking a more stretched conformation of the arms. We observe also that for higher n the hydrodynamic volume of  $PS_nPEMA_n$  is higher to that of  $PS_{2n}$ , whereas the opposite occurs for the lower *n*. The two curves are crossing each other at n close to 6, indicating that the excess volume due to the repulsive interactions between the different arms of the heteroarm star becomes positive beyond a certain number of arms. These results also demonstrate, that in some cases the repulsive interactions may lead to a contraction of the one set of arms (PEMA). This occurs for low n where enough space around the star core still exists. Therefore, in this case the hydrodynamic volume of  $PS_nPEMA_n$  is lower than that of the  $PS_{2n}$ .

By using normalized quantities such as  $\Delta V_R$  and *L* we could compare different  $A_nB_n$  systems in order to look at the influence of the interactions between the A and B arms. Since we have shown that the functionality of the stars affects remarkably the hydrodynamic dimensions of the macromolecule we have kept *n* approximately constant. In

Table 6 Polymer–polymer interaction parameters for PS with various polymers B

Polymer B	$\delta_{\rm PS}~({\rm cal~cm}^{-3})^{1/2}$	$\delta_{\rm B}~({\rm cal~cm}^{-3})^{1/2}$	$\chi_{ ext{PS}- ext{B}}$
PEMA PtBA	9.25 <sup>a</sup> 9.25 <sup>a</sup>	8.85 <sup>a</sup> 8.00 <sup>a</sup>	0.027 0.264
P2VP	9.56 <sup>b</sup>	10.4 <sup>b</sup>	0.119

<sup>a</sup> According to Hoy tables.

<sup>b</sup> According to Van Krevelen tables.

Fig. 7 the behavior of  $PS_nPEMA_n$  is compared with that of  $PS_nPtBA_n$  (Fig. 7(a)) and/or with that of  $PS_nP2VP_n$  (Fig. 7(b)). In the former case two dinstict curves have been obtained belonging to the different systems whereas in the latter case all the points lay in the same curve.

In order to explain qualitatively the above results the Flory–Huggins interaction parameters  $\chi_{AB}$  were calculated by using the formula

$$\chi_{\rm AB} = (\delta_{\rm A} - \delta_{\rm B})^2 V_{\rm r} / RT \tag{15}$$

Where  $\delta_A$  and  $\delta_B$  are the Hildebrand solubility parameters for the A and B arms respectively,  $V_r$  is the reference volume usually taken to be 100 cm<sup>3</sup>/mol and R the gas constant. The solubility parameter of polymers can be estimated from the structural formula using the molar attraction constants  $F_i$ and their densities [19] (Table 6).

To explain the differences in behavior between the systems in Fig. 7, the presence of the solvent must be taken into account. As has been shown recently the repulsive interactions between the different polymers are influenced strongly from the selectivity of the solvent which can be expressed by the difference of the MHS exponents  $\Delta \alpha$ (see Table 4) [20,21]. Therefore the two factors that govern the hydrodynamic volume of the  $A_n B_n$  copolymers are  $\Delta \alpha$ and  $\chi_{AB}$ . For PS<sub>n</sub>PtBA<sub>n</sub>, the estimated  $\chi_{AB}$  value is one order of magnitude higher than that of PS<sub>n</sub>PEMA<sub>n</sub> implying strong incompatibility between the different arms for the former case. The above is further corroborated by a stronger solvent selectivity since  $\Delta \alpha = 0.09$ . As Fig. 7(a) demonstrates this implies much higher hydrodynamic volumes for PS<sub>n</sub>PtBA<sub>n</sub> compared to those for  $PS_nPEMA_n$ . We also observe that the abrupt variation of the hydrodynamic volume of the

heteroarm star for the former system (stage 3) starts at lower L values with respect to the latter one. Furthermore, stage 1, which is extended up to L = 0.45 for PS<sub>n</sub>PEMA<sub>n</sub>, has been shifted now to L = 0.1 for the PS<sub>n</sub>PtBA<sub>n</sub>. Finally the  $\Delta V_R$  for L = 1 is about 1.1 ml for PS<sub>n</sub>PtBA<sub>n</sub> which is even higher than the corresponding PS<sub>2n</sub> (Fig. 6) demonstrating that the strong repulsive interactions even for low star functionality (n = 4.7) provoke significant variation of the dimensions of the heteroarm star copolymer compared to those of the PS<sub>2n</sub>.

It is interest to compare the systems  $PS_nP2VP_n$  and  $PS_nPEMA_n$ . In this case their hydrodynamic behavior coincide (common curve in Fig. 7(b)) although  $\chi_{AB}$  are different. The above results could be attributed to the fact that  $\Delta \alpha$  for both systems are identical and of low magnitude (0.045). As reported by Dondos et al. for the system PS/PMMA/CHCl<sub>3</sub> when  $\Delta \alpha$  becomes 0.05 at 50°C the repulsive interactions are suppressed and compatibily between the two polymers is favored [20]. This resembles our system that exhibits the same level of selectivity. In conclusion we may say that in the case where  $\chi_{AB}$  does not differ very much the key factor affecting the hydrodynamic behavior of the copolymer is the selectivity of the solvent.

#### 4. Conclusions

Size exclusion chromatography was used to characterize the hydrodynamic behavior of the heteroarm star copolymers  $A_n B_n$  in a common good solvent. The proposed method allows the study of the evolution of the hydrodynamic dimensions of the heteroarm star copolymers as the second generation of the arms is growing from the cores. By monitoring the difference  $\Delta V_{\rm R}$  between the retention volumes of the  $A_n B_n$  and  $A_n$  precursor (which is proportional to the normalized hydrodynamic volume of  $A_n B_n$ ) as a function of the dimensionless ratio L of the effective size of the different arm lengths, interesting conclusions have been drawn. The dimensions of  $A_n B_n$  are growing passing several stages depending on the ratio of the effective size of the different arms. In an early stage the size of the heteroarm stars remain stable until a certain length of the second generation of arms is reached. In an intermediate state the  $A_n B_n$  dimensions increase smoothly until the length of the B arms become comparable with that of the A arms. Finally in a prolonged stage the star size increases in a higher rate

since the length of the B arms exceed that of the A arms. The star functionality and the interaction of the unlike segments between the different arms influence remarkably the different stages of the heteroarm star size growth. As the functionality and/or the incompatibility of the different arms increases, these stages occur at lower A,B arm length ratios, L. In other words at a given L the higher the star functionality and/or A,B incompatibility the higher the hydrodynamic volume of the A<sub>n</sub>B<sub>n</sub> star polymer.

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